

Small Signal Parameters:

$$g_m = \frac{2I_D}{V_{OV}} = 1 \text{ mS}$$

$$r_o = \frac{V_A}{I_D} = 200 \text{ k}\Omega$$

$$g_m r_o = 200$$

} All Transistors

1) Minimum V_{out} :

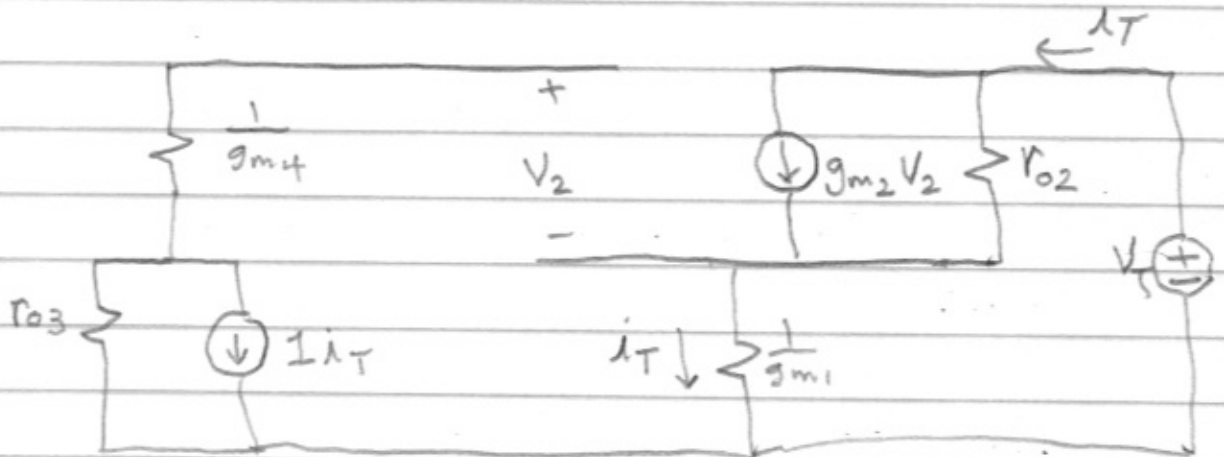
$$V_{out, \min} = V_T + V_{OV1} + V_{OV2} = 0.3 + 0.1 + 0.1 = 0.5 \text{ V}$$

2) R_{out} :

I ignore r_{o4} and r_{o1}

$V_{gs1} = V_{gs3} \rightarrow M3$ mirrors $M1$

These assumptions let us draw the following schematic:



$$i_T = g_{m2} v_2 + \frac{v_T - \lambda_T / g_{m1}}{r_{o2}}$$

$$v_2 = -\lambda_T r_{o3} - \lambda_T / g_{m1}$$

This gives

$$R_{out} = \frac{v_T}{i_T} = r_{o2} \left(1 + \frac{1}{g_{m1} r_{o2}} + r_{o3} g_{m2} + \frac{g_{m2}}{g_{m1}} \right)$$

$$= r_{o2} + \frac{1}{g_{m1}} + r_{o2} g_{m2} \left(1 + \frac{1}{g_{m2} r_{o2}} \right) r_{o3}$$

↑ (EXACT ANSWER) ↑

$$R_{out} = 2 \times 10^5 + 1000 + 200 \left(1 + \frac{1}{200} \right) 2 \times 10^5$$

$$= 4.04 \times 10^7 \Omega$$

often approximated as:

$$R_{out} \cong r_{o2} (1 + g_{m2} r_{o3}) = 4.02 \times 10^7 \Omega$$